## AS Mathematics/Further Maths Summer Work

1 Simplify the following:
a) $p^{3} \times p^{5}$
b) $\left(5 m^{2}\right)^{3}$
c) $\sqrt{ } 192$ (leave in surd form)
d) $\frac{7}{\sqrt{7}} \quad$ (rationalise the denominator)

2 Write as $2^{\mathrm{n}}\left(\operatorname{eg} 8=2^{3}\right)$ :
a) $\mathbf{1 2 8}=$
b) $1=$
c) $8^{4}=$
d) $\frac{1}{4}=$

3 Evaluate $\frac{1}{2}+\frac{x}{3}+\frac{x^{2}}{4} \quad$ when
a) $x=3$
b) $x=1 / 2$
c) $x=-2$

4 If $\mathrm{p}=-1, \mathrm{q}=2$, and $\mathrm{r}=-3$ evaluate:
a) $2 \mathrm{p}-2\left(\mathrm{q}^{2}+\mathrm{r}^{2}\right)$
b) $\frac{(r-q)}{p}+\frac{(3 q-r)}{2 p}$

5 Expand:
a) $5(3 \mathrm{c}-11)$
b) $(3 m-4)(5 m-9)$
c) $(\mathrm{q}-2)^{2}+(\mathrm{q}+3)^{2}$

6 Solve:
a) $5 x+1=2 x+7$
b) $4 x-2(x+1)=5(x+3)+5$
c) $\frac{x+1}{2}+\frac{x-1}{3}=1 / 6$
d) $\frac{3 x}{4}-5=1$

7 Factorise fully:
a) $x^{2}-13 x$
b) $x^{2}-3 x-10$
c) $4 x^{2}+4 x+1$
d) $x^{2}-1$
e) $20 x^{2}-7 x-3$

8 Solve giving your answer to 2 decimal places:
a) $x^{2}+6 x=0$
b) $x^{2}=9 x$
c) $5 x^{2}-7 x-20=0$
d) $4 x^{2}=9 x-3$

9 Solve the equation $x^{2}-6 x+2=0$ by completing the square
10 Make the variable in the square bracket the subject in each of the following:
a) $x^{2}+y^{2}=r^{2}$
[y]
b) $\quad \mathrm{v}=\mathrm{u}+\mathrm{at}$
c) $\mathrm{a}(x-2)=\mathrm{b}(x+1)[x]$
d) $T=2 \pi\left(\sqrt{\frac{l}{g}}\right) \quad[l]$
e) $y=\frac{2 x-4}{x+3}$
[ $x$ ]
f) $r=x-\sin \left(\frac{6}{y}\right) \quad[y]$

11 The sum of three consecutive numbers is 45 .
Find the three numbers, showing your working.

12 Solve the simultaneous equations:

$$
\begin{aligned}
& 2 x+5 y=24 \\
& 4 x+3 y=20
\end{aligned}
$$

Challenge question:
13 Find the sum of

$$
\frac{1}{\sqrt{1}+\sqrt{2}}+\frac{1}{\sqrt{2}+\sqrt{3}}+\text { and so on up to }+\frac{1}{\sqrt{99}+\sqrt{100}}
$$

